# Helix segment assignment in proteins using fuzzy logic 

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#### Abstract

The automatic assignment of protein secondary structure from three dimensional coordinates is an essential step in the characterization of protein structure. Although, the recognition of secondary structures such as alpha-helices and beta-sheets seem straightforward, but there are many different definitions, each regarding different criteria. We have developed a new algorithm for protein helix assignment, by using fuzzy logic based on backbone torsion angles. In this method, each residue takes a number from 0 to 100 that indicates the helical membership degree of that residue. This method can be converted to a classical method whenever we assume that any residue with a membership degree greater than 83 is a helix. Comparison of the results with structures reported in protein data bank (PDB), dictionary of secondary structure of proteins (DSSP) and structure identification (STRIDE) for 324 proteins indicate that our algorithm works as well as DSSP showing 93\% agreement. We believe that the fuzzy secondary structure assignment has more advantages than the other classical approaches used for protein structure comparisons and alignments.


Keywords: Protein structure; Secondary structure assignment; Fuzzy logic.

## INTRODUCTION

The automatic assignment of protein secondary structure from three dimensional coordinates is an essential step in the characterization of protein structure. The

[^0]secondary structure assignment plays an important role in structural genomics. The secondary structure segments are used in protein structure classification (Pearl et al., 2005; Andreeva et al., 2004; Hogue and Bryant, 1998), protein structure alignment (Sternberg et al., 1999; Marti-Renom et al., 2000; Sauder et al., 2000), comparative modeling and threading (Rost, 2000; Rice and Eisenberg, 1997; Kolinski et al., 1999; Xu et al., 1999), and also influence sequence alignment (Smith and Smith, 1992; Fischel-Ghodsian et al., 1993; Henneke, 1989). Although, the recognition of secondary structure such as alpha-helices and betasheets seem straightforward, there are still many different definitions, each regarding different criteria.

The main criteria used in secondary structure assignment are hydrogen bonding patterns known as dictionary of secondary structure of proteins (DSSP) (Kabsch and Sander, 1983), quantification of the back bone curvature (Richards and Kundrot, 1988), inter-c ${ }_{\alpha}$ distances (Levitt and Greer, 1977) and combination of hydrogen bond energy and torsion angle information known as structure identification (STRIDE) (Frishman and Argos, 1995). Comparing these methods on a protein database showed only $63 \%$ agreement between the se three algorithms (Colloc'h et al., 1993). Although, different methods may assign different secondary structure states to each residue, but they are similar in one aspect; each residue is defined in one state and we finally have a string of secondary structure states for the protein sequence. Despite the similarity between an assigned state such as the alpha-helix in different parts of a protein or different proteins, these structures are not exactly the same (Barlow and Thornton, 1988). For example, two alpha-helices with the same length in two different proteins may not have the exact geometrical similarity,
but in the assignment methods this difference is not considered, since most of the protein structure comparison methods are based on secondary structure alignment, renouncement of their geometrical differences leads to an inexact three-dimensional comparison. Thus, it is necessary to define parameters for secondary structures so that different and similar structures can be compared more precisely. In this study, we use fuzzy logic and assign a membership degree to each residue by considering the geometry of consecutive residues with Phi and Psi angles that indicate regular or irregular turns for consecutive residues. These fuzzy numbers may vary from 0 to 100 and can be used to compare two helices for a better similarity or difference.

The exclusive use of backbone torsion angles is not sufficient for assignment of all the secondary structure elements, however, helices' geometry has enough information for detection of helices. Although the algorithm presented in this article is solely based on dihedral angles, results show that the assigned fuzzy numbers identify helical regions of protein structure as good as other classical methods.

## MATERIALS AND METHODS

Representative set of X-ray and NMR protein structures with resolutions better than $2.5 \AA$ and without chain breaks were gathered from the protein data bank (PDB) based on the PDBSELECT list for proteins, with less than $25 \%$ sequence similarity. 324 proteins with 48644 amino acids were selected. These are listed in Table 1.

Alpha-helices assigned by PDB were chosen as standard assignment. Backbone dihedral angles ( $\varphi$ and $\Psi)$ of each residue were taken as in DSSP. From a mathematical point of view, $\Delta$ and $\Delta^{2}$ are approximations of the first and second derivatives. Since our fuzzy algorithm is based on the geometrical structure of helices, and first and second derivatives are tools for studying the plot of a structure, we therefore used $\Delta \varphi$ and $\Delta^{2} \varphi, \Delta \psi$ and $\Delta^{2} \Psi$. To assign a helix fuzzy number to each residue, the following steps were carried out:

1. On all amino acids in the data set, $\Delta \varphi, \Delta \psi, \Delta^{2} \varphi$ and

Table 1. Protein Data Bank (PDB) codes of the Data Set.

| 1a02N | 1ezvA | 1ig3A | 1sfcA | 4sgbE | 1ul7A | 1 ykgA | 1byqA | 1dqeA | 1ep0A | 1gakA | 1if1A | 19g7A |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1aohB | 1f4nA | 1 irdA | 1 sfcB | 5cytR | $1 \mathrm{mmq} A$ | 2asyA | 1bywA | 1dqgA | 1 ete A | 1gd7A | 1im0A | 1qleA |
| 1aoiA | 1fi7A | 1jcqA | 1t3jA | 1 chvS | $1 \mathrm{uph} A$ | 2 axIA | 1c1kA | 1dqiA | 1ew0A | 1gd8A | 1 irdB | 1qmtA |
| 1avyA | 1 fltV | 1jnmA | 1tafB | 1ci5A | $1 \mathrm{uss} A$ | 2azvA | 1c3mA | 1ds1A | 1 excA | 1 gl 2 A | 1 irj A | 1qsoA |
| 1be3A | 1 g 2 cA | 1jqcA | 1tvxA | 1 cirA | 1ut3A | 1a2kA | 1c5fA | 1dxmA | 1 eypA | 1 gl 2 B | 1j4xA | 1qtoA |
| 1bh8A | 1g64A | 1jqIA | 1ty0A | 1 cixA | 1 uvf A | 1a5oA | 1c7kA | 1e30A | 1 f 2 dA | $1 \mathrm{gnh} A$ | 1j75A | $1 q u q A$ |
| 1 bmqA | 1 gcqA | 1 ktzA | 1 uixA | 1cjgA | 1 uw0A | 1 afrA | 1c94A | 1 e 3 kA | 1f46A | 1 gr 3 A | 1j90A | 1sknP |
| 1c8uA | 1gd2E | 11jpA | 1ur6A | 1cl3A | 1 uw 2 A | 1aihA | 1c9iA | 1e44A | $1 f 5 \mathrm{vA}$ | 1h6wA | 1j91A | 1tafA |
| 1cl7L | 1gk4A | 11 lmC | 1 urqA | $1 \mathrm{gcc} A$ | 1uzcA | 1aohA | 1cc8A | 1 e 6 iA | 1 fa 2 A | 1 hciA | 1jejA | 1tc3C |
| 1cxzA | $1 \mathrm{gmj} A$ | 1 ln 1 A | 1 urqB | 1gd4A | 1v06A | 1aq4A | 1 cnoA | 1 ebuA | 1fi2A | $1 \mathrm{hww} A$ | 1jifiA | 1 tgx A |
| 1dazA | 1gqzA | 1 lqvA | 1v54A | 1gh1A | 1v1cA | 1 atIA | 1cqmA | 1ec5A | $1 \mathrm{fl7B}$ | 1 hxrB | 1jgsA | 1tiid |
| 1df4A | 1gu4A | 1 mspA | 1vkkA | 1gh5A | $1 \mathrm{v1dA}$ | 1avoA | 1cqxA | 1 ecsA | 1 flk A | 1hziA | 1ji6A | 1t\|2A |
| 1dj7A | 1guxA | 1no4A | 1wapA | 1gh8A | 1 v 2 yA | 1ayoA | 1cqyA | 1 eczA | 1 flmA | 1i07A | 1jmvA | 1 tvxB |
| 1dm9A | 1h2sA | 1oczA | 1 wmsA | 1gh9A | 1v31A | 1b0nA | 1 cvmA | 1ed1A | 1 fltW | 1 i 4 mA | 1jyoA | 1 kkrA |
| 1dp5A | 1h3qA | 1qg7B | 1xbrA | 1ghhA | 1v32A | 1b3aA | 1d8eA | 1ee6A | 1 fp 2 A | 1i4sA | 1k04A | 1 ycqA |
| 1dpsA | 1h80A | 1qn2A | 1xdtT | 1 gjtA | 1v38A | 1b4uA | 1d8uA | 1eggB | 1fs7A | 1i4wA | 1k20A | 2 cpgB |
| 1 dtd A | 1 hcfA | 1qnaB | 1ycpL | 1 gjxA | 1 v 3 a A | 1b66A | 1d9uA | 1 ehkA | 1 fvzA | 1i4zA | 1 k 2 fA | 2eboA |
| 1e1hA | 1hxrA | 1qnaA | 1ytbA | 1go1A | 1v3fA | 1b9xA | 1dazC | 1ej3A | 1fx8A | $1 i 5 g A$ | 1 krqA | $2 h r v A$ |
| 1e44B | 1hynP | 1qrvA | $2 \mathrm{cpg} A$ | 1 uilA | 1 v 5 kA | 1 bfeA | 1dcpA | 1ej8A | 1 fzcA | 1 i 8 a | 1 ktzB | 2thiA |
| 1e7kA | 1hyrB | 1r26A | 2hddA | 1 ujdA | 1v5IA | 1bh9A | 1debA | 1ejeA | 1fzhA | 1 i 8 nA | 1 mkaA | 3 ygsP |
| 1 eaiA | 1i1rA | 1 r 3 j A | 2occA | 1ujoA | 1 v 5 mA | 1bkrA | 1 dfnA | 1ejfA | 1 fzrA | 199bA | 1mr8A |  |
| 1 eayA | 1i78A | 1 r 4 xA | 2 sivA | 1 ujrA | 1 v 5 rA | 1 bnIA | 1 dfuP | 1 lm A | 1 g 5 zA | 1iazA | 1p35A |  |
| 1eg4P | 1 i 1 IA | 1r7jA | 3caaA | 1 ujt A | 1v61A | 1 bpIA | 1dm9B | 1elwA | 1g6uA | 1ib5A | 1 pcfA |  |
| 1 l ggA | 1ic2A | 1 ryhA | 3ygsC | 1ujvA | 1v63A | 1bqcA | 1dmhA | 1 mmvA | 1g8kA | 1 ibyA | 1qb3A |  |
| 1 euvA | 1 idrA | 1scjA | 4fapA | 1uk5A | 1v65A | 1bxaA | 1dp7P | 1eoiA | 1g9zA | 1id1A | 1 qftA |  |

$\Delta^{2} \psi$ for each residue were calculated as follow:
$\Delta \varphi(\mathrm{n})=\left\{\begin{array}{l}\min \{|\varphi(\mathrm{n})-\varphi(\mathrm{n}-1)| \cdot|\varphi(\mathrm{n})-\varphi(\mathrm{n}+1)|\} \\ \frac{|\varphi(\mathrm{n})-\varphi(\mathrm{n}-1)|+|\varphi(\mathrm{n})-\varphi(\mathrm{n}+1)|}{2}\end{array}\right.$
if $-100 \leq \varphi(n) \leq 0$
Otherwise
$\Delta \psi(\mathrm{n})=\left\{\begin{array}{lc}\min \{|\psi(\mathrm{n})-\psi(\mathrm{n}-1)| .|\psi(\mathrm{n})-\psi(\mathrm{n}+1)|\} & \text { if }-100 \leq \psi(\mathrm{n}) \leq 0 \\ \frac{|\psi(\mathrm{n})-\psi(\mathrm{n}-1)|+|\psi(\mathrm{n})-\psi(\mathrm{n}+1)|}{2} & \text { Otherwise }\end{array}\right.$
$\Delta^{2} \varphi(\mathrm{n})=\frac{\mid \Delta(\varphi(\mathrm{n}))-\Delta(\varphi(\mathrm{n}-1)|+|\Delta(\varphi(\mathrm{n}))-\Delta(\varphi(\mathrm{n}+1))|}{2}$
$\Delta^{2} \psi(\mathrm{n})=\frac{\mid \Delta(\psi(\mathrm{n}))-\Delta(\psi(\mathrm{n}-1)|+|\Delta(\psi(\mathrm{n}))-\Delta(\psi(\mathrm{n}+1))|}{2}$
Where n is denoted as the $\mathrm{n}^{\text {th }}$ amino acid in the protein.
2. Amino acids which are not located in the helix domain of the Ramachandran plot and with the following conditions were excluded from the data set.
$\left\{\begin{array}{c}-180 \leq \varphi \leq 0 \\ 64.5 \leq \psi \leq 180\end{array}\right.$ or $\left\{\begin{array}{c}-180 \leq \varphi \leq 0 \\ -180 \leq \psi \leq-153\end{array}\right.$
These residues form the set A.
3. All of the segments assigned as alpha-helix by PDB, with lengths more than seven residues were selected. Three residues from the N-cap and three residues from the C-cap were excluded and averages of $\Delta^{2} \varphi$ and $\Delta^{2} \Psi$ for the remaining residues were calculated and denoted by $\alpha_{\varphi}$ and $\alpha_{\Psi}$, respectively.
4. For all residues in the helix state, in the data set with $\Delta^{2} \varphi \geq \alpha_{\varphi}$, average of $\varphi$ was calculated and named $\ell_{1, \varphi} \cdot \ell_{1, \psi}$ was also calculated as above for $\Psi$ angles. Hence, $\ell_{\varphi}$ and $\ell_{\psi}$ parameters are defined as:

$$
\begin{aligned}
& \ell_{\varphi}=2 \ell_{1, \varphi}-\alpha_{\varphi} \\
& \ell_{\psi}=2 \ell_{1, \psi}-\alpha_{\psi}
\end{aligned}
$$

In fact $\alpha_{\varphi}$ and $\alpha_{\Psi}$ denote the maximum variations allowed for a helix to be considered as a standard helix. Similar to the rational behind a $95 \%$ confidence interval for a mean in a normal distribution, we consider a confidence region for an amino acid to be in a helix structure, based on $\ell_{\psi}$ and $\ell_{\varphi}$ simultaneously. It should be mentioned here that the information on amino acids discarded in step 3 , is now being considered at this stage. This means no information has been missed. Since we are only interested in helix structure, therefore, all those amino acids considered in steps 3 (internal) and 4 (C- cap and N cap) are not to be considered.
5. $f_{\varphi}$ and $f_{\Psi}$ functions were defined as follows:

$$
\left.\begin{array}{c}
\mathrm{f}_{\varphi}(\mathrm{n})= \begin{cases}100 & \text { if } 0 \leq \Delta^{2} \varphi(\mathrm{n}) \leq \alpha_{\varphi} \\
\frac{100\left(\ell_{\varphi}-\Delta^{2} \varphi(\mathrm{n})\right)}{\ell_{\varphi}-\alpha_{\varphi}} & \text { if } \alpha_{\varphi} \leq \Delta^{2} \varphi(\mathrm{n}) \leq \ell_{\varphi}\end{cases} \\
\text { Otherwise }
\end{array}\right\} \begin{array}{ll}
100 & \text { if } 0 \leq \Delta^{2} \psi(\mathrm{n}) \leq \alpha_{\psi} \\
\mathrm{f}_{\psi}(\mathrm{n})= \begin{cases}\frac{100\left(\ell_{\psi}-\Delta^{2} \psi(\mathrm{n})\right)}{\ell_{\psi}-\alpha_{\psi}} & \text { if } \alpha_{\psi} \leq \Delta^{2} \psi(\mathrm{n}) \leq \ell_{\psi} \\
0 & \text { Otherwise }\end{cases}
\end{array}
$$

finally function $f$ gives the fuzzy value for helicity according to the following formulation:

$$
f(n)=\left\{\begin{array}{l}
\frac{f_{q}(n)+f_{\psi}(n)}{2} \\
0
\end{array}\right.
$$

$$
\begin{aligned}
& \text { if residue was not in set } \mathrm{A} \\
& \text { if residue was in set } \mathrm{A}
\end{aligned}
$$

## RESULTS AND DISCUSSION

Analysis of helix regularity using variation in the consecutive residue dihedral angles $\varphi$ and $\psi$ gives the helix fuzzy number for each residue, between 0 to 100 . Table 2 shows these numbers for two proteins. In this table helix assignment by PDB, DSSP, STRIDE, with fuzzy numbers greater than also 83 being compared. Usually the central residues of helices take numbers close to 100 , and N - and C - terminal residues of each helix take lower values and show less regularity. Consecutive residues with the same or near fuzzy numbers show the regular helix turn, although it may be far from the standard helix structure. Segments with fuzzy numbers close to 100 are regular helices with standard helix geometries. Helix distortion has been studied in detail and can be attributed to factors such as solvent-side chain interactions, local sequence and side chain packing (Barlow and Thornton, 1998). However, these factors cause the residues in helices to have different major chain conformations and such distortions could be shown by differences in consecutive dihedral angles.

Figure 1 shows the superposition of fragments assigned as helices by PDB with the same length and different or same fuzzy numbers using the CE program (http://cl.sdsc.edu/) (Shindyalov and Bourne, 1998). Root mean square (RMS) calculation shows a relation between fuzzy numbers and geometry of compared helices. Two superposed helices with the same fuzzy numbers show less RMS which increases when the fuzzy numbers of two helices are different. These assigned fuzzy numbers for residue helicity, in addi-

Table 2. Fuzzy numbers for parts of two proteins and comparison of assigned helices by PDB, DSSP, STRIDE with fuzzy numbers greater than 83 .

| PDB Code | Residue No. | AA | $\Phi$ | $\psi$ | PDB | DSSP | STRIDE | Fuzzy | $\begin{gathered} \text { fuzzy } \\ \text { number } \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 tafA | 1 | P | 360 | -46.7 |  |  | H |  | 0 |
| 1 tafA | 2 | K | -60.4 | -46.67 | H | H | H |  | 24 |
| 1 tafA | 3 | D | -71.63 | -33.94 | H | H | H | H | 98 |
| 1 tafA | 4 | A | -61.48 | -40.57 | H | H | H | H | 95 |
| 1 tafA | 5 | Q | -63.2 | -42.66 | H | H | H | H | 100 |
| 1 tafA | 6 | V | -60.52 | -44.64 | H | H | H | H | 100 |
| 1tafA | 7 | I | -63.5 | -38.7 | H | H | H | H | 100 |
| 1 tafA | 8 | M | -66.31 | -35.52 | H | H | H | H | 100 |
| 1 tafA | 9 | S | -69.6 | -37.58 | H | H | H | H | 100 |
| 1tafA | 10 | I | -64.63 | -43.23 | H | H | H | H | 100 |
| 1 tafA | 11 | L | -58.14 | -44.84 | H | H | H | H | 100 |
| 1 tafA | 12 | K | -68.43 | -43.9 | H | H | H | H | 100 |
| 1 tafA | 13 | E | -61.57 | -31.72 | H | H | H | H | 95 |
| 1 tafA | 14 | L | -92.67 | 18.81 |  |  | H | H | 94 |
| 1 tafA | 15 | N | 62.46 | 32.33 |  |  |  |  | 50 |
| 1 tafA | 16 | V | -100.04 | 89.05 |  |  |  |  | 0 |
| 1 tafA | 17 | Q | -71.16 | -28.82 |  |  |  |  | 34 |
| 1 tafA | 18 | E | -135.82 | 139.22 |  |  |  |  | 0 |
| 1 tafA | 19 | Y | -157.47 | 154.29 |  |  |  |  | 0 |
| 1 tafA | 20 | E | -66.29 | 138.8 |  |  |  |  | 0 |
| 1 tafA | 21 | P | -51.5 | -38.42 | H |  | H |  | 61 |
| 1 tafA | 22 | R | -66.37 | -10.64 | H | H | H | H | 94 |
| 1 tafA | 23 | V | -62.41 | -39.91 | H | H | H | H | 88 |
| 1 tafA | 24 | V | -61.19 | -43.74 | H | H | H | H | 100 |
| 1 tafA | 25 | N | -60.59 | -47.54 | H | H | H | H | 100 |
| 1 tafA | 26 | Q | -56.4 | -43.61 | H | H | H | H | 100 |
| 1 tafA | 27 | L | -71.13 | -30.13 | H | H | H | H | 99 |
| 1 tafA | 28 | L | -71.39 | -36.28 | H | H | H | H | 100 |
| 1 tafA | 29 | E | -67.91 | -38.07 | H | H | H | H | 100 |
| 1 tafA | 30 | F | -64.85 | -46.8 | H | H | H | H | 100 |
| 1 tafA | 31 | T | -52.22 | -48.2 | H | H | H | H | 96 |
| 1 tafA | 32 | F | -63.38 | -45.89 | H | H | H | H | 95 |
| 1 tafA | 33 | R | -61.87 | -43.52 | H | H | H | H | 100 |
| 1 tafA | 34 | Y | -66.58 | -51.07 | H | H | H | H | 100 |
| 1 tafA | 35 | V | -62.33 | -44.79 | H | H | H | H | 100 |
| 1 tafA | 36 | T | -63.88 | -38.44 | H | H | H | H | 100 |
| 1 tafA | 37 | S | -62.64 | -47.57 | H | H | H | H | 100 |
| 1 tafA | 38 | I | -64.34 | -44.48 | H | H | H | H | 100 |
| 1 tafA | 39 | L | -66.32 | -34.26 | H | H | H | H | 100 |
| 1 tafA | 40 | D | -62.57 | -39.36 | H | H | H | H | 100 |
| 1 tafA | 41 | D | -77.4 | -42.75 | H | H | H | H | 94 |
| 1 tafA | 42 | A | -57.04 | -35.34 | H | H | H | H | 95 |
| 1 tafA | 43 | K | -62.26 | -37.52 | H | H | H | H | 100 |
| 1 tafA | 44 | V | -64.43 | -44.47 | H | H | H | H | 100 |
| 1 tafA | 45 | Y | -61.78 | -43.66 | H | H | H | H | 100 |
| 1 tafA | 46 | A | -61.67 | -40.22 | H | H | H | H | 100 |
| 1 tafA | 47 | N | -61.9 | -50.3 | H | H | H | H | 98 |
| 1tafA | 48 | H | -65.91 | -15.55 | H | H | H | H | 99 |
| 1 tafA | 49 | A | -97.48 | -5.11 |  |  | H | H | 85 |
| $1 \mathrm{taf} A$ | 50 | R | 63.92 | 50.68 |  |  |  |  | 11 |
| 1tafA | 51 | K | -118.09 | 153.71 |  |  |  |  | 0 |
| 1 tafA | 52 | K | -97.6 | -24.84 |  |  |  |  | 44 |
| 1 tafA | 53 | T | -115.29 | 129.16 |  |  |  |  | 0 |
| 1tafA | 54 | 1 | -65.54 | 131.73 |  |  |  |  | 0 |

Table 2. Continue

| PDB Code | Residue No. | AA | $\Phi$ | $\psi$ | PDB | DSSP | STRIDE | Fuzzy | fuzzy number |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2hddA | 1 | R | 360 | 98.14 |  |  | C |  | 0 |
| 2 hddA | 2 | T | -56.81 | 156.48 |  |  | C |  | 0 |
| 2hddA | 3 | A | -122.02 | 109.92 |  |  | C |  | 0 |
| 2 hddA | 4 | F | -64.56 | 141.64 |  |  | C |  | 0 |
| 2hddA | 5 | S | -78.2 | 150.34 |  |  | C |  | 0 |
| 2 hddA | 6 | S | -60.71 | -17.65 | H | H | H |  | 62 |
| 2 hddA | 7 | E | -74.65 | -39.48 | H | H | H | H | 87 |
| 2hddA | 8 | Q | -72.48 | -47.52 | H | H | H | H | 100 |
| 2 hddA | 9 | L | -57.22 | -36.55 | H | H | H | H | 93 |
| 2hddA | 10 | A | -70.11 | -34.6 | H | H | H | H | 97 |
| 2hddA | 11 | R | -75.58 | -39.4 | H | H | H | H | 100 |
| 2 hddA | 12 | L | -63.44 | -44.31 | H | H | H | H | 99 |
| 2hddA | 13 | K | -64.21 | -40.69 | H | H | H | H | 100 |
| 2hddA | 14 | R | -65.51 | -37.31 | H | H | H | H | 100 |
| 2 hddA | 15 | E | -71.47 | -42.55 | H | H | H | H | 99 |
| 2hddA | 16 | F | -59.23 | -39.56 | H | H | H | H | 100 |
| 2 hddA | 17 | N | -65.6 | -36.03 | H | H | H | H | 100 |
| 2 hddA | 18 | E | -74.17 | -42.78 | H | H | H | H | 100 |
| 2hddA | 19 | N | -150.93 | 110.74 |  |  | T |  | 0 |
| 2 hddA | 20 | R | -75.14 | -7.7 |  | S | T | H | 85 |
| 2hddA | 21 | Y | -122.12 | 129.73 |  | S | T |  | 0 |
| 2hddA | 22 | L | -84.17 | 146.57 |  |  | T |  | 0 |
| 2 hddA | 23 | T | -100.18 | 163.94 |  |  | C |  | 0 |
| 2hddA | 24 | E | -60.51 | -41.43 | H | H | H |  | 33 |
| 2hddA | 25 | R | -63.75 | -46.86 | H | H | H | H | 100 |
| 2 hddA | 26 | R | -66.22 | -39.88 | H | H | H | H | 99 |
| 2hddA | 27 | R | -59.23 | -38.93 | H | H | H | H | 99 |
| 2 hddA | 28 | Q | -66.89 | -44.56 | H | H | H | H | 96 |
| 2hddA | 29 | Q | -66.63 | -38.52 | H | H | H | H | 100 |
| 2hddA | 30 | L | -67.87 | -39.93 | H | H | H | H | 100 |
| 2 hddA | 31 | S | -57.68 | -50.17 | H | H | H | H | 97 |
| 2hddA | 32 | S | -59.15 | -63 | H | H | H | H | 100 |
| 2 hddA | 33 | E | -57.53 | -35.04 | H | H | H | H | 95 |
| 2 hddA | 34 | L | -93.27 | -10.4 | H | H | H | H | 86 |
| 2hddA | 35 | G | 68.66 | 49.19 |  | T | C |  | 15 |
| 2 hddA | 36 | L | -134.64 | 163.67 |  |  | C |  | 0 |
| 2hddA | 37 | N | -77.92 | 148.18 |  |  | C |  | 0 |
| 2hddA | 38 | E | -58.92 | -29.2 | H | H | H |  | 44 |
| 2 hddA | 39 | A | -67.15 | -33.47 | H | H | H | H | 99 |
| 2 hddA | 40 | Q | -71.2 | -37.64 | H | H | H | H | 100 |
| 2hddA | 41 | I | -63.97 | -48.95 | H | H | H | H | 100 |
| 2 hddA | 42 | K | -55.1 | -47.67 | H | H | H | H | 100 |
| 2hddA | 43 | 1 | -70.52 | -30.37 | H | H | H | H | 92 |
| 2hddA | 44 | W | -71.78 | -42.86 | H | H | H | H | 97 |
| 2 hddA | 45 | F | -64.27 | -39.37 | H | H | H | H | 100 |
| 2hddA | 46 | K | -62.29 | -46.72 | H | H | H | H | 100 |
| 2 hddA | 47 | N | -70.3 | -34.17 | H | H | H | H | 98 |
| 2 hddA | 48 | K | -64.31 | -49.57 | H | H | H | H | 99 |
| 2 hddA | 49 | R | -53.59 | -42.44 | H | H | H | H | 99 |
| 2 hddA | 50 | A | -67.6 | -36.55 | H | H | H | H | 96 |
| 2hddA | 51 | K | -65.26 | -49.54 | H | H | H | H | 98 |
| 2hddA | 52 | I | -59.03 | -34.39 | H | H | H | H | 94 |
| 2 hddA | 53 | K | -60.14 | -34.46 | H | H | H | H | 100 |
| 2hddA | 54 | K | -101.5 | 51.26 |  | T | H |  | 35 |
| 2hddA | 55 | S | -96.32 | 360 |  |  | C |  | 43 |

A

 | 1HMNA | 84 | 91 | 100 | 100 | 100 | 100 | 99 | 100 | 100 | 99 | 100 | 100 | 100 | 98 | 99 | 100 | 100 |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1MKAA | 100 | 100 | 100 | 100 | 100 | 100 | 99 | 100 | 100 | 99 | 100 | 100 | 100 | 100 | 100 | 100 | 100 |
| 99 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | $\mathrm{RMSD}=0.5 \mathrm{~A}$

B

c

$\begin{array}{lrrrrrrrrrrrrrrrrrr}\text { 1HWWA } & 84 & 91 & 100 & 100 & 100 & 100 & 99 & 100 & 100 & 99 & 100 & 100 & 100 & 98 & 99 & 100 & 100 & 99 \\ \text { 1J90A } & 0 & 92 & 99 & 100 & 100 & 100 & 100 & 100 & 100 & 100 & 100 & 71 & 45 & 0 & 89 & 98 & 98 & 94\end{array}$ $\mathrm{RMSD}=2.6 \mathrm{~A}$

Figure 1. Superposition of helices with the same length and different or same fuzzy numbers, with their RMSD for residues 310-327 of 1HWWA, 79-96 of 1MKAA (A) 715-732 of 1HCIA (B) and 156-173 of $1 \mathrm{~J} 90 \mathrm{~A}(\mathrm{C})$.
tion to showing helix regularity can be used for comparison and alignment of protein structures. Instead, those with are based on a string of secondary structure elements in which each residue is defined as belonging to one state or another, and where the regularity and geometry of secondary structure is ignored. Fuzzy numbers also show helicity for small segments with
lengths of two or three residues that although are not classified as helices, but share similar geometry with the helix. However, the main goal of this method is assignment of a helical fuzzy number to each residue, but it can also be simply converted to the classical method involving the assignment of a residue with helical or non-helical structure. For this purpose, residues with fuzzy numbers greater than a threshold number k , were assigned as H and others as $\boldsymbol{H}$. In a five residue length window, if one H is surrounded by four $\boldsymbol{H s}$, it can be converted to $\boldsymbol{H}$ and vice versa. Allowing k to vary, we can find all helix structures near to or far from the standard helix structure. For example, for k close to 100 , the helix structures near to the standard are found and if k was far from 100 , we detect the structure far from the standard. In order to compare with PDB, we look for a certain k for which the correlation coefficient of data generated by our algorithm after using the threshold number k and those generated by PDB are maximized. This leads to $\mathrm{k}=83$. Comparisons of the results with the crystallographer's assignments as percentage of correctly assigned residues in two states (helix or non-helix) are $90 \%$ for all amino acids in the dataset.

Comparison of DSSP with our method shows that they have $94 \%$ agreement for H and $\boldsymbol{H}$. Although many of the crystallographers define secondary structure based on the DSSP algorithm, comparison of DSSP and PDB assigned secondary structures in our dataset show $8 \%$ differences between them. Analysis of differences between results of this study and DSSP showed that 1342 residues were assigned by the method of this study to H , while DSSP assigned them to $\boldsymbol{H}$. There were 1783 residues that our method assigned to $\boldsymbol{H}$, while DSSP assigned them to H . Comparison of our method and STRIDE show approximately $94 \%$ agreement for H and $\boldsymbol{H}$. Table 3 shows the details of comparisons between the method described heae with PDB, DSSP and STRIDE and also comparisons of DSSP and STRIDE with PDB. Most of

Table 3. Comparison of results obtained by fuzzy logic and other methods.

| Compared methods | TP $^{1}$ | TN $^{2}$ | FP $^{3}$ | FN $^{4}$ | Tot | $\%$ | Sensitivity | Specificity | CC $^{5}$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Fuzzy and PDB | 16822 | 26912 | 1200 | 3710 | 48644 | 89.9 | 81.9 | 93.3 | 0.79 |
| Fuzzy and DSSP | 15009 | 30510 | 1342 | 1783 | 48644 | 93.6 | 89.4 | 91.8 | 0.86 |
| Fuzzy and STRIDE | 15366 | 30175 | 1090 | 2013 | 48644 | 93.6 | 88.4 | 93.4 | 0.86 |
| DSSP and PDB | 16712 | 28035 | 80 | 3820 | 48644 | 91.98 | 81.4 | 99.5 | 0.84 |
| STRIDE and PDB | 17096 | 27832 | 283 | 3436 | 48644 | 92.36 | 83.3 | 98.4 | 0.85 |

${ }^{1}$ True positive (TP), ${ }^{2}$ True negative (TN), ${ }^{3}$ False Positive (FP), ${ }^{4}$ False negative (FN), ${ }^{5}$ Correlation Coefficient (CC).
the false positive and negative assignments between method of this study and PDB occurred at the edges of helices. Although the major assumption of this work is that helices can be defined by fuzzy logic and instead of assigning each residue to one state, it may be assigned by a fuzzy number which is far more valuable for comparing protein structures. However, this approach can also be used in the classical assignment of helix structure. The results obtained are as good as DSSP and STRIDE algorithms, which are the most widely used methods for secondary structure assignment.

In this article the main goal was only fuzzy number assignment to helices followed by demonstration of their regularities. Fuzzy number assignment to other secondary structures such as beta-strands and turns can be the subject of an independent work and in fact we are developing a method for fuzzy assignment of secondary structures. For this reason the title "Helix segment assignment in proteins using fuzzy logic" was selected for this article.

It is also believed that the combination of dihedral angles and other parameters such as H -bonds can lead to a different method with better results which can also be the subject of an other independent work.

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